

## Math 105 Assignment 9

Due the week of March 28

1. Recall problem 3 from Homework 8, the monopolist selling two products in Canada and the UK. Let  $x$  be the number of units to be sold in Canada and  $y$  the number of units to be sold in the UK. Due to the laws of demand and in order to sell all the units, the monopolist must set the unit price at  $97 - (x/10)$  dollars in Canada and  $83 - (y/20)$  dollars in the UK. The cost of production is \$3 per unit, in addition to a base capital of \$20,000. Suppose due to a new regulation he must now set the same price per unit in each country. Find the values of  $x$  and  $y$  that maximize profit under this new restriction.

(5 points)

2. Suppose that a firm makes two products  $A$  and  $B$  that use the same raw materials. Given a fixed amount of raw materials and a fixed amount of manpower, the firm must decide how much of its resources should be allocated to the production of  $A$  and how much to  $B$ . The management is aware of the *production possibilities curve*

$$9x^2 + 4y^2 = 18,000$$

which reflects the limitations on personnel and raw materials available to the firm. A point  $(x, y)$  on this curve is called a *production schedule* for the firm, committing it to produce  $x$  units of  $A$  and  $y$  units of  $B$ . The sale of each unit of  $A$  yields a \$3 profit, whereas each unit of  $B$  yields a \$4 profit. Assuming that all units produced are sold, find the production schedule that maximizes the profit of the firm.

(5 points)

3. Roger is breeding tropical fish to sell to hobbyists. He feels that his supply curve looks like

$$y_1 = 0.06x^2 + 5.06,$$

where  $x$  is the number of fish, in hundreds, sold at  $y_1$  dollars each. Articles in his trade newsletters lead him to believe that the demand curve is given by the portion of the quadratic curve

$$y_2 = 0.2x^2 - 4.8x + 31.8$$

that is a decreasing function of  $x$ .

- (a) Check that the equilibrium quantity is 7. Calculate the producer surplus if Roger sells at  $y_1(7)$ .
- (b) What is the consumer surplus?

(5 points)