Math 101 – WORKSHEET 21 SEPARABLE DIFFERENTIAL EQUATIONS

1. What is a DE?

- (1) Consider the differential equation $y' = 3y^2$ (a) For which values of C, D is $f(x) = Cx^D$ a solution to the equation?
 - (b) Suppose f(x) is a solution. Show that f(x-a) is also a solution for any a. What is the solution with f(0) = 1?

2. Separation of variables

(2) Solve the following equations using separation of variables (a) $y' = x^3$

(b) y' = 5y

(c) (Final, 2012) y' = xy, y(0) = e.

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(3) (Final 2014) Find the solution of the DE $x \frac{dy}{dx} + y = y^2$ that satisfies y(1) = -1.

- (4) A physical system satisfies the equation $\frac{1}{2}mv^2 + \frac{1}{2}kx^2 = E$. There m, k, E are constants (mass, spring constant, energy, respectively) and $v = \frac{dx}{dt}$ is the velocity. (a) Solve the equation to obtain $\frac{dx}{dt} = v =$

(b) Suppose m = k = 1 and $E = \frac{1}{2}$. Integrate both sides of $\frac{dx}{\sqrt{1-x^2}} = dt$ and find a formula for x = x(t).

⁽c) Solve the problem for general m, k, E.