

**Math 101 – WORKSHEET 33**  
**TAYLOR SERIES AND DERIVATIVES**

The *Taylor series* of  $f(x)$  centered at  $a$  is

$$\sum_{n=0}^{\infty} \frac{f^{(n)}(a)}{n!} (x - a)^n$$

(1) Find the MacLaurin series of  $f(x) = e^x$ .

(2) (Final 2014) Find the Taylor series  $g(x) = \log x$  centered at  $a = 2$ , as well as its radius of convergence.

(3) (Final 2014) Let  $\sum_{n=0}^{\infty} c_n x^n$  be the MacLaurin series for  $e^{3x}$ . Find  $c_5$ .

(4) (Final 2013) Let  $f(x) = x^2 \sin(x^3)$ . Find  $f^{11}(0)$ .