

Math 101 – WORKSHEET 30
POWER SERIES

(1) Which of the following is a power series:

$$\square \sum_{n=0}^{\infty} \frac{n!(x-3)^n}{2^{2^n}} \quad \square \sum_{n=0}^{\infty} \frac{3}{n!} (e^x)^n$$

1. THE INTERVAL OF CONVERGENCE

(2) Find the radius of convergence and interval of convergence of the power series

(a) $\sum_{n=1}^{\infty} (-1)^{n-1} \frac{(x-1)^n}{n}$

(b) $\sum_{n=0}^{\infty} n!x^n$

(c) $\sum_{n=0}^{\infty} \frac{x^n}{n!}$

(d) (Final, 2014) $\sum_{n=0}^{\infty} \frac{(x-2)^n}{n^2+1}$

(e) (Final, 2011) $\sum_{n=0}^{\infty} \frac{(x-2)^n}{\log(n+2)}$

