# Math 101 - WORKSHEET 24 SERIES 

1. Skill 1: Geometric series and decimal expansions
(1) (Final 2013) Find the sum of the series $\sum_{n=2}^{\infty} \frac{3 \cdot 4^{n+1}}{8 \cdot 5^{n}}$. Simplify your answer.
(2) Express each decimal expansion using a geometric series, sum the series, then simplify to obtain a rational number.
(a) $0.333333 \ldots$
(b) $0.5757575757 \ldots$
(c) $0.6545454545454 \ldots$

## 2. Skill 2: Telecoping series

(3) Write an expression for the partial sums, decide if the series converges, and if so determine the sum. (a) $\sum_{n=1}^{\infty} \frac{2}{n(n+2)}$
(b) $\sum_{n=0}^{\infty}(\tan (n)-\tan (n+1))$
(c) $\sum_{n=1}^{\infty}\left(n^{2}-(n+1)^{2}\right)$

