## MATH 253 - WORKSHEET 15 DIRECTIONAL DERIVATIVES

(1) An ant is crawling along the curve $y=x^{2}$ at the rate of $v \mathrm{~cm} / \mathrm{s}$ (distances are measured in cm ). The temperature in the $x y$ plane is varying according to $T(x, y)=\frac{y}{1+x^{2}}$. What is the rate of change of the temperature the ant sees when it is located at $(x, y)$ ?
(2) Show that every plane tangent to the surface $z^{2}=x^{2}+y^{2}$ passes through the origin.

